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A mechanism of photocatalytic and adsorptive treatment of 2,4-dinitrophenol on a porous thin film of $TiO₂$ covering granular activated carbon particles

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ABSTRACT

The present work investigates the mechanism of the photocatalytic and adsorptive treatment of an aqueous DNP (2,4-dinitrophenol) solution in an annular-flow reactor installed with a TiO₂/AC-PET film (a polyethylene terephthalate film adhesively fixing activated carbon particles covered with a thin and porous film of titanium dioxide). Unfortunately, the experimental result indicates that it is impossible to correctly measure the time courses of product ion concentrations because they are adsorbed onto or desorbed from AC particles. Therefore, a computer simulation methodology using mathematical models is introduced in order to elucidate the treatment mechanism. Treatments of aqueous DNP solutions using the TiO₂-PET film reveal that the diffusion of DNP from a bulk solution to a TiO₂ film is based on the gradient of DNP concentration, generated by a rapid adsorption of DNP onto AC and photocatalytic reaction, in the very neighborhood of $TiO₂ film$, and this diffusion increases the DNP concentration at the surface of TiO₂ film, thereby enhancing the rate of photocatalytic decomposition. Moreover, it is found that the TiO2/AC-PET film can lower the burden of the adsorption of DNP onto AC compared with the AC-PET film because a part of DNP molecules are photocatalytically decomposed and the percentage of this decomposition is increased at a lower linear velocity. In conclusion, the mathematical model taking into consideration a film-diffusional effect can successfully explain the complicated mechanism of the treatment of an aqueous DNP solution using the $TiO₂/AC-PET$ film.

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1. Introduction

A number of wastewaters containing various kinds of organic compounds are treated by microbial decomposition processes. When the wastewaters contain organic compounds highly toxic to microbial cells, however, introduction of some other method must be considered [\[1–4\].](#page-8-0) For example, wastewaters containing 2,4-dinitrophenol (DNP), which is mainly used as a raw material of black dyes, polymerization inhibitor, and wood preservative, significantly restrict cell growth even when the DNP concentration level is of the order of 1 ppm (parts per million). According to the PRTR (Pollutant Release and Transfer Register) data in 2007, it is estimated that DNP of about 0.38 tons per year was released into the environment in Japan [\[5\].](#page-8-0)

Titanium dioxide (TiO₂) irradiated with UV light can decompose a wide variety of organic compounds to carbon dioxide, water, and mineral acids or their salts [\[3,6,7\].](#page-8-0) Hence, the decomposition method using $TiO₂$ has a potential for the treatment of wastewaters containing toxic organic compounds such as DNP [\[1,2,4,8–10\].](#page-8-0) Unfortunately, it is not easy to enhance the rate of photocatalytic decomposition to a level of practical application because $TiO₂$ does not sufficiently adsorb organic compounds, especially when they are hydrophobic.

To solve this problem, many researchers have attempted to combine $TiO₂$ with adsorptive materials such as activated carbon (AC) and zeolite particles [\[4,11–14\]. A](#page-8-0) high photocatalytic activity may be achieved if the surface area of $TiO₂$ per unit volume is successfully increased. One of the best ways is to completely cover the surface of adsorptive materials with a $TiO₂$ film in order to get as much field for the photocatalytic reaction as possible. In this case, however, the adsorption ability of AC particles cannot be utilized efficiently.

In a previous work [\[15\], w](#page-8-0)e prepared a $TiO₂/AC-PET film$, where the surface of AC particles adhesively fixed onto a PET film was completely covered with a porous and thin film of $TiO₂$ crystal particles in large sizes, and investigated its performance for the treatment of an aqueous DNP solution. As a result, we found that the $TiO₂/AC-$ PET film can rapidly treat it compared to a $TiO₂$ -PET film where the TiO2 particles were directly loaded onto a PET film. Interestingly, in this reaction system, the rate of a decrease in the DNP concentration by the $TiO₂/AC-PET$ film without UV irradiation was almost

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the same as that by the AC-PET film. This finding implies that the adsorption ability of AC is not weaken in the presence of the $TiO₂$ film because it is very thin and porous. In addition, the $TiO₂/AC-$ PET film was able to treat a 1.8 times larger amount of DNP than did the AC-PET film until AC on each PET film was saturated with DNP. This experimental fact suggests that DNP may be decomposed at a higher reaction rate by the TiO₂/AC-PET film than by the TiO₂-PET film, because the DNP concentration on the $TiO₂/AC-PET$ film would be more increased by a high attraction force of AC; consequently, the burden of AC adsorption of DNP is lowered and a larger amount of DNP can be treated by the $TiO₂/AC-PET$ film than by the AC-PET film.

The purpose of the present work is to elucidate the mechanism of the photocatalytic and adsorptive treatment of DNP using the $TiO₂/AC-PET film$. To achieve this purpose, the scheme of the photocatalytic decomposition of DNP is firstly investigated on the basis of the decomposition experiment using the $TiO₂$ -PET film. Secondly, the treatment of DNP using the $TiO₂/AC-PET$ film is experimentally analyzed, which indicates that there is a limitation to experimental elucidation of its mechanism. Therefore, mathematical models are constructed to theoretically elucidate the mechanism of the photocatalytic and adsorptive treatment.

2. Experimental method

2.1. Materials

DNP used as a reactant was purchased fromWako Pure Chemical Industries, Ltd. (Osaka, Japan). A nonionic surfactant (polyoxyethylene lauryl ether with a degree of polymerization of 23) used to increase the affinity of an aqueous $TiO₂$ coating solution to a PET film was also the product of Wako Pure Chemical Industries, Ltd. The coating solution (aqueous H_2O_2 solution) containing anatase TiO $_2$ fine particle in sizes of 10–25 $\rm \mu m$ was a product of Sundecor Co. Ltd. (Fukuoka, Japan). The details of this coating solution are described elsewhere [\[16\]. A](#page-8-0) 6-W blacklight blue fluorescent lamp (Matsushita Electric Industrial Co., Ltd., Osaka, Japan; FL6BL-B) was used as a light source of UV light (wavelengths; 300–400 nm). Granular AC particles in sizes of roughly 1-2 mm were purchased from Japan EnviroChemicals Ltd. (WH2CSS; Osaka, Japan).

2.2. Preparations of TiO₂-, AC- and TiO₂/AC-PET films

Polyethylene terephthalate (PET) films, 0.085 m \times 0.195 m in size and 0.01 mm thick, were used as supports of $TiO₂$, AC and AC coated with $TiO₂$. The preparation methods are detailed elsewhere [\[15\]. I](#page-8-0)n the following, the PET film covered with a thin film of TiO₂ is referred to as TiO₂-PET film, the PET film where AC particles are adhesively fixed onto its surface is referred to as AC-PET film, and the PET film where the surface of the AC particles adhesively fixed is completely covered with a thin film of $TiO₂$ is referred to as TiO₂/AC-PET film. The weights of TiO₂ loaded on TiO₂- and $TiO₂/AC-PET$ films were determined to be about 0.09 and 0.12 g, respectively. However, since the measured weight for the $TiO₂/AC-$ PET film includes the weight of water absorbed into AC particles, we consider that there is not remarkable difference between the amounts of TiO₂ loaded on the TiO₂- and TiO₂/AC-PET films.

2.3. Experimental procedures

The removal experiments of DNP from aqueous solutions were conducted in a batch-recirculation system with an annular-flow photocatalytic reactor [\[17–21\]](#page-8-0) as shown in [Fig. 1. T](#page-2-0)he plastic photocatalytic reactor consists of a cylindrical vessel (0.20 m long and 0.0285 m in inlet diameter), a 6-W blacklight blue fluorescent lamp, a quartz glass tube (0.024 m in outer diameter) used for protection of the UV lamp, and a PET film with $TiO₂$ and/or AC particles. The photocatalytic reactor was connected with a mixed-flow container via a peristaltic pump (RP-2; EYELA, Tokyo, Japan) as shown in [Fig. 1.](#page-2-0) A reaction mixture flows through an annulus between the inside wall of the cylindrical vessel and the outside wall of the quartz glass tube. The PET film was inserted into the annulus so that it contacts closely to the inside wall of the cylindrical vessel. The volume of the annulus in the photocatalytic reaction zone was 3.7×10^{-5} m³.

A 5.0 \times 10⁻⁴ m³ aqueous solution of DNP at different initial concentrations was poured into the mixed-flow container and then circulated at different flow rates. The UV lamp was switched on to start the photocatalytic reaction. At appropriate time intervals, an aliquot of the reaction mixture in the mixed-flow container was withdrawn to determine the DNP concentration by measurement of an absorbance at 357 nm with a spectrophotometer (Ultrospec 1100Pro; Amersham Biosciences, Sweden). The concentrations of ions ($NO₂^-$, $NO₃^-$, $NH₄^+$, and $CO₃^{2-}$) produced during the DNP decomposition were determined by ion chromatography (ICS 90; Japan Dionex, Osaka, Japan).

3. Mathematical models

3.1. Constitution of reaction systems and characteristics of experimental data

The present work treats DNP solutions in a batch-recirculation mode. That is, a reaction mixture of the volume V_L in a mixed-flow container is circulated by passing through an annular-flow photocatalytic reactor. The rate of recirculation is very large compared to the rate of decomposition (the rate of treatment). Therefore, the present treatment can be approximately regarded as a batch mode, which means that the reactant concentration profile along the reactor can be neglected [\[22,23\]. O](#page-8-0)n the other hand, the experimental data given in a previous paper [\[15\]](#page-8-0) possess the following characteristics.

- (1) There is no significant difference between the time courses of DNP concentrations in bulk solutions in the treatments of aqueous DNP solutions using the $TiO₂/AC-PET$ film without UV irradiation and the AC-PET film. This means that the thin film of TiO₂ covering the surface of AC particles on the TiO₂/AC-PET film hardly lowers the ability of AC to attract DNP.
- (2) In repeated treatments of aqueous DNP solutions, the amount of DNP required to saturate the AC on the $TiO₂/AC-PET$ is 1.8 times larger than that on the AC-PET film. This means that the burden of the adsorption of DNP on AC is lowered as a result of photocatalytic decomposition of DNP.

The mathematical models to be constructed must be satisfied with these facts.

3.2. Mathematical model for decomposition of DNP using a TiO2-PET film

In the batch-recirculation annular-flow reactor installed with a $TiO₂$ -PET film, reactant molecules diffuse through a liquid film from a bulk solution to a photocatalyst surface excited with UV light and are then decomposed photocatalytically. The present system is kept at a steady state and the flux of reactant molecules diffusing through the liquid film is equal to the rate of decomposition on the $TiO₂$ film. Thus, a differential mass balance gives

$$
-V_L \frac{dC_b}{dt} = k_{Lp} A_s (C_b - C_p)
$$
\n(1)

Fig. 1. Schematic of a batch-recirculation flow system with an annular-flow reactor installed with a TiO₂-, AC-, or TiO₂/AC-PET film.

$$
V_P \frac{dC_p}{dt} = k_{LP} A_s (C_b - C_p) - \frac{k_p V_p K_H C_p}{1 + K_H C_p} = 0
$$
\n(2)

with the initial conditions:

$$
C_b = C_{b0}
$$
, $C_p = C_{p0} = 0$, at $t = 0$

where k_p [mmol m⁻³ – cat min⁻¹] is the rate constant of the photocatalytic decomposition, K_H [mmol⁻¹ m³] is the adsorption equilibrium constant, C_p [mmol m⁻³] is the DNP concentration at the TiO₂ surface, k_{Lp} [m min⁻¹] is the mass-transfer coefficient for the diffusion of DNP through a liquid film in the photocatalytic reaction system, C_b [mmol m⁻³] is the DNP concentration in a bulk solution, V_L [m³] is the volume of a reaction mixture, A_s [m² cat] is the area of a plane perpendicular to the direction of diffusion, V_p $[m³ cat]$ is the volume of the TiO₂ film, and t [min] is the reaction time. Also, the subscript "0" represents the value at $t = 0$, namely, the initial value. Solving Eq. (2) with respect to C_p and substituting the obtained equation into Eq. [\(1\)](#page-1-0) gives a differential equation that is a function of only C_h . The time course of C_h is obtained by numerically solving this differential equation. If there is no filmdiffusional resistance, i.e., if $k_{Lp} = \infty$, Eqs. [\(1\) and \(2\)](#page-1-0) is simplified to the following kinetic equation:

$$
\upsilon_p = -\frac{dC_b}{dt} = \frac{(k_p/V_L)V_pK_HC_b}{1 + K_HC_b} \tag{3}
$$

with the initial condition:

$$
C_b = C_{b0}, \quad \text{at } t = 0.
$$

where ν_p [mmol m $^{-3}$ min $^{-1}$] is the photocatalytic reaction rate. The values of k_p and K_H are determined from a linearized plot based on the initial rates of decomposition ν_{p0} measured at various initial reactant concentrations C_{b0} .

3.3. Mathematical model for adsorption of DNP onto an AC-PET film

In the batch-recirculation annular-flow reactor installed with an AC-PET film, the DNP concentration is decreased as a result of AC adsorption of DNP. A differential mass balance gives [\[24\]](#page-8-0)

$$
-V_L \frac{dC_b}{dt} = k_{La} A_s (C_b - C_a e^{\lambda_a}) = V_a \frac{dC_a}{dt}
$$
\n(4)

with the initial conditions:

$$
C_b = C_{b0}
$$
, $C_a = C_{a0} = 0$, at $t = 0$

where C_a [mmol m⁻³] is the DNP concentration on AC particles, k_{La} [m min⁻¹] is the mass-transfer coefficient for the diffusion of DNP through a liquid film in the AC adsorption system, λ_a is the partition coefficient for DNP at the surface of AC particles, and V_a $[m³]$ is the volume of AC particles. In general, it may be possible to express k_{La} and k_{Lp} in terms of the same mass-transfer coefficient. However, the surface condition of the TiO₂- and TiO₂/AC-PET films are markedly different, which would give subtle differences in the thicknesses of diffusion film and the surface areas for diffusion. For simplification, therefore, the present work distinguishes and sets up them as different mass-transfer coefficients. Eq. (4) provides the following equation expressing a relationship between C_a and C_b .

$$
C_a = \left(\frac{V_L}{V_a}\right)(C_{b0} - C_b) \tag{5}
$$

Substitution of Eq. (5) into Eq. (4) gives

$$
\frac{dC_b}{dt} + \frac{k_{La}A_s}{V_L} \left(1 + \frac{V_L e^{\lambda_a}}{V_a}\right) C_b = \frac{k_{La}A_s e^{\lambda_a}}{V_a} C_{b0}
$$
(6)

Eq. (6) is a linear first-order differential equation, whose analytical solution leads to

$$
C_b = C_{b0} \left(\frac{V_a}{V_a + V_L e^{\lambda_a}} \right) \exp \left[-\frac{k_{La} A_s (V_a + V_L e^{\lambda_a})}{V_a V_L} t \right] + C_{b,eq} \tag{7}
$$

$$
C_{b,eq} = \frac{C_{b0} V_L e^{\lambda_a}}{V_a + V_L e^{\lambda_a}}
$$
\n
$$
(8)
$$

Firstly, the final reactant concentrations in a bulk solution, i.e., equilibrium reactant concentrations, $C_{b,eq}$, must be obtained from the time course data of C_b in the treatments of aqueous DNP solutions at different values of C_{b0} . Secondly, the values of $C_{b,eq}$ are plotted against the values of C_{b0} to obtain the value of λ_a from the slope of the linear plot of Eq. (8). Finally, k_{La} is determined so that the calculated result by Eq. (7) agrees with the time course data of C_b .

3.4. Mathematical model for adsorption and decomposition of DNP on a TiO₂/AC-PET film

The $TiO₂/AC-PET$ film is set in the annular-flow reactor to treat an aqueous solution containing DNP in the batch-recirculation flow system. The $TiO₂$ film covering the surface of AC particles hardly lowers the ability of AC particles to attract DNP, because it is thin and porous. The DNP concentration in the very neighborhood of the TiO₂/AC-PET film is significantly reduced due to a rapid adsorption of DNP onto AC and its photocatalytic decomposition, so that the DNP molecules can quickly diffuse to the neighborhood of the PET film by utilization of a large concentration gradient as a driving force. The DNP concentration at the $TiO₂$ film is higher than

that in its neighborhood because of solid–liquid partition. About half of the DNP molecules on the TiO₂ film would be photocatalytically decomposed and the others would be quickly attracted and adsorbed onto AC. The DNP concentration at the TiO₂ film is higher with $TiO₂/AC-PET$ film than with $TiO₂-PET$ film because the flux of DNP passing through the porous $TiO₂$ film becomes larger as a result of quick attraction of DNP by AC. This in turn increases the rate of photocatalytic decomposition of DNP. Not only undecomposed DNP molecules but also a part of intermediates produced by DNP decomposition are adsorbed on AC. This series of process including diffusion, partition, photocatalytic decomposition, and AC adsorption is described as follows:

$$
-V_L \frac{dC_b}{dt} = k_{La}A_s(C_b - C_p e^{\lambda_p}) + k_{La}A_s(C_b - C_a e^{\lambda_a})
$$
\n(9)

$$
V_p \frac{dC_p}{dt} = k_{La} A_s (C_b - C_p e^{\lambda_p}) - \frac{k_p V_p K_H C_p}{1 + K_H C_p}
$$
(10)

$$
V_a \frac{dC_a}{dt} = k_{La} A_s (C_b - C_a e^{\lambda_a})
$$
\n(11)

with the initial conditions:

$$
C_b = C_{b0}
$$
, $C_p = C_{p0} = 0$, $C_a = C_{a0} = 0$, at $t = 0$

where λ_p is the partition coefficient for DNP at the TiO₂ film. Eqs. (9)–(11) simply describe an increase in the DNP concentration in the neighborhood of the TiO₂ film, which is caused by the adsorption ability of AC, in terms of a partition phenomenon.

3.5. Catalytic effectiveness factor

The catalytic effectiveness factor, E_f in a photocatalytic reaction system is written as [\[17,18\]](#page-8-0)

$$
E_f = \frac{\text{Actual rate of decomposition}}{\text{Ideal rate of decomposition in absence of diffusional resistance}}
$$
\n
$$
= \frac{v_p(C_p)}{v_p(C_b)} = \frac{V_p K_H C_p/(1 + K_H C_p)}{V_p K_H C_b/(1 + K_H C_b)} = \frac{\beta_p/(1 + \beta_p)}{\beta_b/(1 + \beta_b)}.
$$
\n(12)

Eq. [\(2\)](#page-2-0) gives the following equation for the dimensionless DNP concentration at the $TiO₂$ surface:

$$
\beta_p = \frac{-(\phi + 1 - \beta_b) + \sqrt{(\phi + 1 - \beta_b)^2 + 4\beta_b}}{2} \tag{13}
$$

where $\beta_p = C_p K_H$, $\beta_b = C_b K_H$, and $\phi = k_p V_p K_H / (k_{Lp} A_s)$. Application of Eq. (13) to Eq. (12) gives the equation of E_f as

$$
E_f = \frac{(\beta_b + 1)(\beta_b + \phi + 1 - \sqrt{(\phi + 1 - \beta_b)^2 + 4\beta_b})}{2\phi\beta_b}.
$$
 (14)

Consequently, the rate of decomposition of DNP for the $TiO₂$ -PET film is described as

$$
\upsilon_p = -\frac{dC_b}{dt} = E_f \frac{(k_p/V_L)V_pK_HC_b}{1 + K_HC_b} \tag{15}
$$

3.6. Mass-transfer coefficient

In general, the mass-transfer coefficient k_L is expressed as a function of the linear velocity u for a reaction mixture passing through the inside of a photocatalytic reactor, given [\[18,25,26\]](#page-8-0) by

$$
k_L = a u^b \tag{16}
$$

where *a* and *b* are the experimental constants determined from the initial rates of treatments based on the time courses of the DNP concentrations in the treatments of aqueous DNP solutions at a constant concentration under different conditions of linear velocity. The determination method of a and b is described elsewhere [\[18,25\].](#page-8-0)

Fig. 2. Time courses of DNP and product ion concentrations in treatment of an aqueous solution of DNP at an initial concentration of 57.6 mmol m[−]³ using a TiO2-PET film at a linear velocity of 0.55 m min[−]1.

4. Results and discussion

4.1. Decomposition of DNP using a TiO₂-PET film

A 0.5 \times 10⁻⁴ m³ aqueous solution of DNP at an initial concentration of 57.6 mmol m^{-3} was treated using the annular-flow reactor installed with a TiO₂-PET film at a linear velocity of 0.55 m min⁻¹. Fig. 2 shows the time courses of DNP, CO_3^2 ⁻, NO_2^- NH₄⁺, and NO₃⁻ concentrations in this treatment. No photolysis of DNP was found under irradiation with UV light from the blacklight blue fluorescent lamp. The DNP concentration decreased to an almost zero value in 8h. At the same time, the $NO₃⁻$ concentration increased quickly and reached a value over 70 mmol m^{−3} after 24 h. The $NO₂$ ⁻ concentration initially increased, passing through a maximum at about 2 h and decreasing to an almost zero value after 8 h. This behaviour suggests that $NO₂⁻$ is an intermediate in a consecutive decomposition reaction. The NH₄⁺ concentration quickly increased until 4 h, reaching its maximum and then staying at the neighborhood of its value. The CO $_3{}^{2-}$ concentration stayed at an almost zero value until 6h, increasing and taking a constant value of about 10 mmol m^{-3} after 24 h. This result suggests slow decompositions of intermediates produced from DNP.

Consequently, the photocatalytic decomposition of DNP is estimated to occur according to the reaction mechanism shown in Fig. 3. The fundamental of this reaction mechanism was proposed by Nakano et al. [\[4\]. T](#page-8-0)he reaction mechanism in Fig. 3 is a combination of their mechanism with our experimental results that nitro groups are quickly eliminated from DNP, while intermediates produced from DNP are slowly decomposed to $CO₃^{2−}$.

Fig. 3. A reaction mechanism estimated for photocatalytic decomposition of DNP.

Fig. 4. Time courses of DNP and product ion concentrations in treatment of aqueous solutions of DNP at an initial concentration of 54.5 mmol m[−]³ at a linear velocity of 0.55 m min⁻¹: (A) fresh TiO₂/AC-PET film and (B) a repeatedly used TiO₂/AC-PET film.

4.2. Effect of ions adsorbed on a TiO₂/AC -PET film

A 0.5×10^{-4} m³ aqueous solution, containing NO₃⁻, NO₂⁻, $CO₃²⁻$ and NH₄⁺ at initial concentrations of 14.1, 13.3, 37.5, and 5.5 mmol m[−]3, respectively, was treated using 5 g of suspended fresh granular AC particles under vigorous mixing for 2 h. The experimental result suggested that the fresh AC particles originally contain CO₃^{2–} and NH₄⁺ (especially contain CO₃^{2–} in large amounts) and these ions may be solved out into the liquid solution during the DNP treatment. On the other hand, $NO₃$ ⁻ and $NO₂$ ⁻ are not or slightly contained in the fresh AC particles. It is therefore presumed that if the experiment of DNP decomposition is repeated using the same TiO₂/AC-PET film, the ions such as $NO₃^-$, $NO₂^-$, $CO₃²⁻$ and NH₄⁺ adsorbed on AC particles affect the time courses of the concentrations of ions produced during the photocatalytic reaction.

Fig. 4 shows the time courses of DNP and product ion concentrations in the treatment of an aqueous solution of DNP at an initial concentration of 54.5 mmol m⁻³ using a fresh TiO₂/AC-PET film (left figure; A) and a repeatedly used TiO₂/AC-PET film (right figure; B). As predicted from the experimental fact stated above, the $CO₃^{2–}$ concentration remarkably increased during the treatment because this ion was originally contained in AC particles and supposed to be released from them (Fig. 4(A)). Since the AC particles on the TiO₂/AC-PET film were adhesively fixed onto one side of the PET film, the total amount of CO₃^{2–} released is smaller than that released when AC particles were suspended in an aqueous solution. The NH4 ⁺ concentration also increased. It is obvious that the time courses of these concentrations were influenced by the concentrations of ions produced by the DNP decomposition and originally contained in the AC particles. On the other hand, the fresh AC particles do not or slightly contain $NO₃⁻$ and $NO₂⁻$. It is therefore presumed that most of these ions produced during the photocatalytic decomposition were adsorbed onto the AC particles. This makes it hard to quantitatively identify the time courses of product ion concentrations from the experimental data for fresh AC particles. The DNP concentration in Fig. 4(B) decreased more slowly than did the experimental result in Fig. 4(A), because repetitive use of the $TiO₂/AC-PET$ film caused a drop in the adsorption capacity of AC. However, it decreased faster than did the $TiO₂$ -PET film. Because most of CO₃^{2–} originally contained in the AC particles had already been solved out as a result of repetitive use of the $TiO₂/AC-$ PET film, its concentration was not remarkably increased in this experimental run, although this time course data is also presumed to have been more or less influenced by adsorption of ions onto the AC particles. The $NO₃$ and $NO₂$ concentrations were kept at almost zero values during the treatment of Fig. 4(A), whereas they increased continuously or decreased to a zero value after increasing, as shown in Fig. 4(B). The time course data evidently includes an influence of AC adsorption and therefore, it is impossible to conduct quantitative discussion. However, it is obvious that photocatalytic decomposition of DNP certainly occurred.

In a previous work [\[15\],](#page-8-0) we found that the $TiO₂/AC-PET$ film can treat an 1.8 times larger amount of DNP until AC is saturated with DNP than can do the AC-PET film. The $TiO₂/AC-PET$ film also decreased the DNP concentration at an initial rate 2.86 times larger than that observed with the $TiO₂$ -PET film (compare [Fig. 2](#page-3-0) with Fig. 4). These results suggest that the DNP concentration at the $TiO₂$ surface on the $TiO₂/AC-PET$ film becomes higher because of rapid diffusion of DNPmolecules, so that it decomposes DNPmore rapidly than does the $TiO₂$ -PET film. As shown above, however, the present photocatalytic and adsorptive treatment is strongly influenced by the adsorption and desorption of product ions. It is thus difficult to experimentally elucidate the mechanism of the treatment. In the following, therefore, we will introduce a computer simulation methodology using mathematical models.

4.3. Investigation of reaction mechanisms based on mathematical models

A $TiO₂$ -PET film was used to determine initial rates of decomposition of DNP at different initial concentrations. Aqueous DNP solutions were recirculated at a high linear velocity where the filmdiffusional resistance can be neglected. In the treatment of aqueous solutions using a TiO₂-PET film at linear velocity of 0.78 m min⁻¹, the following linear relationship between C_{b0}/v_{p0} and C_{b0} was found under the assumption of Langmuir–Hinshelwood kinetics.

$$
\frac{C_{b0}}{\nu_{p0}} = 158.7 + 0.864 C_{b0}
$$
\n(17)

The kinetic parameters were determined from the slope and intercept of this equation as $k_p = 350$ mmol m⁻³ min⁻¹ and K_H = 0.0055 m³ mmol⁻¹. These values were inserted into Eq. [\(3\)](#page-2-0) and this equation with $V_L = 5.0 \times 10^{-4}$ m³ was numerically solved to obtain the time course of DNP concentration. The calculated line is shown by a solid line in [Fig. 5, w](#page-5-0)here the experimental data were obtained from the decomposition of DNP at an initial concentration of 54.5 mmol m⁻³ using the TiO₂-PET film at $u = 0.78$ m min⁻¹.

Fig. 5. A time course of DNP concentration in treatment of an aqueous DNP solution at an initial concentration of 54.5 mmol m[−]³ using a TiO2-PET film at a linear velocity of 0.78 m min[−]1. The calculated line by Eq. [\(3\)](#page-2-0) is shown by a solid line.

The calculated result is in a good agreement with the experimental data.

Fig. 6 shows the time courses of DNP concentrations in the treatments of DNP solutions at various initial concentrations using the AC-PET film at $u = 0.55$ m min⁻¹. Adsorption of organic compounds onto AC can usually be described by the Langmuir adsorption isotherm. In general, the adsorption reaches equilibrium after the passage of a sufficiently long time and the concentrations of organic compounds finally become constant. The equilibrium DNP concentrations $C_{b,eq}$ were obtained from Fig. 6 and plotted against the initial concentrations C_{b0} . Obviously there is a linear relationship between $C_{b,eq}$ and C_{b0} . The slope value of the straight line was calculated and applied to Eq. [\(8\).](#page-2-0) This calculation with V_L = 5.0 × 10⁻⁴ m³ and V_a = 2.5 × 10⁻⁵ m³ provided −7.33 for λ_a . All the obtained values were further applied to Eq. [\(7\)](#page-2-0) to calculate the time course of C_b . In this case, the value of k_{La} was changed so that the calculated results were fitted to the time course data at different initial DNP concentrations in Fig. 6. Consequently, k_{La} was obtained as 4.90×10^{-4} m min⁻¹. The calculated results shown by

Fig. 6. Time courses of DNP concentrations in treatments of aqueous DNP concentrations at different initial concentrations using an AC-PET film at a linear velocity of 0.55 m min[−]1. The calculated lines by Eq. [\(7\)](#page-2-0) are shown by solid lines.

Fig. 7. Relationships of initial reaction rate and linear velocity in treatments of aqueous DNP solutions using a TiO₂- and AC-PET film at initial concentration of 54.5 mmol m⁻³. The calculated lines for the TiO₂- and AC-PET films are shown by broken and solid lines, respectively.

solid lines in Fig. 6 are in good agreements with the experimental data.

Fig. 7 shows the relationship between the initial rate of treatment and the linear velocity in the treatments of aqueous DNP solutions at an initial DNP concentration of 54.5 mmol m⁻³ using $TiO₂$ - and AC-PET films. The initial rate for the AC-PET film greatly increased almost linearly with an increase of u. On the other hand, the initial rate for the TiO₂-PET film increased slightly with an increase of u in its small region and approached a constant rate at u above 0.5 m min⁻¹. Its initial rate is considerably small compared to the initial rate for the AC-PET film. It is therefore clear that the adsorptive treatment of DNP using the AC-PET film is more rapid than the photocatalytic treatment using the TiO₂-PET film.

Fig. 8 shows the plot of the mass-transfer coefficients, which were determined from the experimental data in Fig. 7 by the convergence method, against the linear velocities. In this calculation, the volume of the TiO₂ thin film was set as $V_p = 1.66 \times 10^{-6}$ m³, which was calculated by setting the surface area of the TiO₂ film as

Fig. 8. A relationship between mass-transfer coefficient and linear velocity in treatments of aqueous DNP solutions using a $TiO₂$ - and AC-PET film at initial con-centration of 54.5 mmol m⁻³. The calculated lines by Eq. [\(18\)](#page-6-0) for the TiO₂-PET film and by Eq. (19) for the AC-PET film are shown by broken and solid lines, respectively.

 A_s = 0.0166 m² and its film thickness as 1×10^{-4} m as a result of SEM observation of the TiO₂ film. When u is less than 0.75 m min⁻¹, the mass-transfer coefficient for the AC-PET film, i.e., k_{La} , is larger, while when u is larger than 0.75 m min⁻¹, the mass-transfer coefficient for the TiO₂-PET film, i.e., k_{Lp} , becomes larger. This is because in the treatment of DNP using the $TiO₂$ -PET film, the rate of photocatalytic decomposition of DNP is small relative to the rate of diffusion of DNP and the treatment system therefore becomes reaction-limited for a smaller value of the linear velocity. As a result of applying a least-square method to the plotted data in [Fig. 8, t](#page-5-0)he equation for the mass-transfer coefficient was determined as

$$
k_{Lp} = 0.000698u^{1.39}
$$
 (18)

for the $TiO₂$ -PET film and as

$$
k_{La} = 0.000897u^{0.842} \tag{19}
$$

for the AC-PET film.

Eq. [\(14\)](#page-3-0) was used to calculate the relationship of u and E_f in the treatments of aqueous DNP solutions at an initial concentration of 54.5 mmol m⁻³ using the TiO₂-PET film. At u below 0.3 m min⁻¹, E_f was smaller than 0.5 because the film-diffusional resistance was large. At u larger than 1 m min⁻¹, on the other hand, E_f increased with an increase of u and then exceeded 0.9, implying that the system was reaction-limited.

Fig. 9 shows the time course of DNP concentrations in the treatments of aqueous DNP solutions at various initial concentrations using the TiO₂/AC-PET film at $u = 0.55$ m min⁻¹. A comparison of these experimental data with those in [Fig. 6](#page-5-0) indicates that the DNP concentration for the $TiO₂/AC-PET$ film is decreased more quickly than that for the AC-PET film. This is because a part of DNP molecules rapidly diffusing by means of the adsorption power of AC are photocatalytically decomposed on the $TiO₂$ surface. Consequently, the DNP concentration in the neighborhood of the PET film is more decreased, which subsequently causes an increase in the diffusion flux of DNP and a quicker decrease in the DNP concentration in the bulk solution. To construct a mathematical model that is best fitted to these experimental data, we firstly investigated the performance of the following differential equation where the rate of decrease in the DNP concentration in the bulk solution occurs only by the diffusion based on the concentration gradient generated by the adsorption power of AC.

$$
-V_L \frac{dC_b}{dt} = k_{La} A_s (C_b - C_a e^{\lambda a})
$$
\n(20)

Fig. 9. Time courses of DNP concentrations in treatments of aqueous DNP concentrations at different initial concentrations using a $TiO₂/AC-PET$ film at a linear velocity of 0.75 m min[−]1. The calculated lines by Eqs. [\(9\)–\(11\)](#page-3-0) are shown by solid lines.

This equation provides a maximum for the rate of diffusion when the second term on the right-hand side is zero. Unfortunately, every calculated line was found to locate above the corresponding time course data at different initial DNP concentrations in Fig. 9. This result suggests that the diffusion of DNP from the bulk solution to the support surface is not simply dependent on the adsorption power of AC.We therefore added an effect of the DNP concentration decreased by the photocatalytic decomposition to Eq. (20) (see Eq. [\(9\)\)](#page-3-0) and investigated the performance of this modified equation. The value of λ_p was changed so that the calculated results by Eqs. [\(9\)–\(11\)](#page-3-0) were fitted to the experimental data in Fig. 10. As a result, we obtained -1.0 for λ_p .

Fig. 10 shows the simulation results by Eqs. (9) – (11) for the time courses of amounts of DNP adsorbed onto AC using an AC-PET film and photocatalytically decomposed using a $TiO₂/AC-PET$ film the treatments of aqueous DNP solutions at an initial concentration of 54.5 mmol m⁻³ at $u = 0.1$ and 0.55 m min⁻¹. It is clear that TiO₂ decomposes a half of DNP molecules at $u = 0.1$ and three tens at $u = 0.55$ m min⁻¹. The amount of DNP decomposed by TiO₂ becomes larger when u is smaller. This is because when u is small, DNP diffuses more slowly, which increases a probability that DNP molecules are captured and decomposed by $TiO₂$ before they are

Fig. 10. Simulations of time courses of amounts of DNP adsorbed onto AC using an AC-PET film and photocatalytically decomposed using a TiO2/AC-PET film in treatments of aqueous DNP solutions at an initial concentration of 54.5 mmol m−³ at a linear velocity of 0.1 m min−¹ (left) and 0.55m min−¹ (right).

Fig. 11. Comparisons of time courses of DNP concentration in bulk solutions (left column) and at a photocatalyst surface (right column) in treatments of DNP solutions at an initial concentration of 54.5 mmol m⁻³ using TiO₂- and TiO₂/AC-PET films at a linear velocity of 0.1 m min⁻¹ (upper line) and 0.5 m min⁻¹ (lower line).

adsorbed onto AC. The photocatalytic decomposition of DNP by $TiO₂$ would lower the burden of the adsorption of DNP onto AC on the $TiO₂/AC-PET$ film. This explains the experimental result that the lifetime of AC on the $TiO₂/AC-PET$ film was 1.8 times longer than that of AC on the AC-PET film [\[15\]. F](#page-8-0)rom the findings that the calculated results shown by solid lines in [Fig. 9](#page-6-0) were in good agreements with the experimental data and the calculated result agreed with the experimental observation concerning the lifetime of AC, it is obvious that the mathematical model constructed for the treatment of an aqueous DNP solution using the $TiO₂/AC-PET$ film is reasonable.

Fig. 11 compares the simulations for the treatments of aqueous DNP solutions at an initial concentration of 54.5 mmol m−³ using the TiO₂/AC- and TiO₂-PET films at $u = 0.1$ and 0.5 m min⁻¹. In both cases of linear velocities, the DNP concentrations in the bulk solution for the $TiO₂/AC-PET$ film decrease more quickly than those for the $TiO₂$ -PET film. This characteristic is more pronounced as u is smaller. The DNP concentration at the TiO₂ thin film on the $TiO₂/AC-PET$ film is large in the initial stage of the decomposition. This is because in the initial stage, a large amount of DNP molecules rapidly diffuse by means of the adsorption power of AC, which leads to an increase in the DNP concentration not at the surface of but in the neighborhood of $TiO₂$ thin film. This concentration thereafter decreases rapidly, then becomes smaller than the DNP concentration at the TiO₂ film on the TiO₂-PET film, and finally approaches a zero value. At a low linear velocity, the DNP concentration at the $TiO₂$ film on the TiO₂/AC-PET film would initially become high compared to that at the TiO₂ film on the TiO₂-PET film. This suggests that when u is small, the TiO₂/AC-PET photocatalytically decomposes a larger amount of DNP molecules than does the $TiO₂$ -PET film. This finding is useful for the wastewater treatment using $TiO₂$

excited with sunlight because the use of a smaller linear velocity is advantageous for energy saving.

The experimental results indicate that the $TiO₂/AC-PET$ film irradiated with UV light can efficiently decompose DNP because DNP diffuses quickly owing to the adsorption power of AC and its concentration increases in the very neighborhood of the support. When the film-diffusional resistance is large, the percentage of DNP molecules decomposed by $TiO₂$ is increased compared to that adsorbed onto AC. There was no mathematical model simultaneously describing both the photocatalytic decomposition and AC adsorption under the condition where the AC surface is completely covered with a $TiO₂$ film but the adsorption power of AC is not remarkably lost. The mathematical model constructed here simply expresses the increases in the DNP concentration at the surfaces of AC and TiO₂, caused by the AC adsorption and photocatalytic decomposition of DNP, in terms of partition phenomena. Nevertheless, the calculated results indicate that the present model can successfully explain the treatment of an aqueous DNP solution using the $TiO₂/AC-PET$ film.

5. Conclusions

In the first stage of the present work, we experimentally investigated the mechanism of the treatment of an aqueous DNP solution using TiO₂-, AC-, and TiO₂/AC-PET films. As a result, the following conclusions are drawn.

- (1) Elimination of nitro groups from DNP occurs quickly.
- (2) Decomposition of intermediates produced from DNP into $CO₃^{2–}$ occurs slowly. Unfortunately, it was impossible to correctly measure the time courses of the concentrations of

product ions because they were adsorbed onto or desorbed from AC particles. In the second stage, therefore, we performed computer simulations using mathematical models. As a result, the following conclusions are drawn.

- (3) In the treatment of an aqueous DNP solution at an initial concentration of 54.5 mmol m⁻³ using the TiO₂-PET film, the effectiveness factor takes a value more than 0.9 at a linear velocity above 1 m min−¹ and the present system becomes reaction-limited.
- (4) In the treatment of an aqueous DNP solution using the $TiO₂/AC-$ PET film, the diffusion of DNP from a bulk solution to a TiO₂ film is based on the gradient of DNP concentration, generated as a result of the AC adsorption and photocatalytic decomposition of DNP, in the very neighborhood of $TiO₂ film$.
- (5) This diffusion increases the DNP concentration at the surface of $TiO₂$ film, thereby enhancing the rate of photocatalytic decomposition.
- (6) Moreover, the burden of the adsorption of DNP onto AC is lowered compared to its treatment using the AC-PET film because a part of DNP molecules are photocatalytically decomposed and the percentage of this decomposition is increased at a lower linear velocity.
- (7) The mathematical model taking into consideration a filmdiffusional effect can successfully explain the complicated mechanism of the treatment of an aqueous DNP solution using the TiO2/AC-PET film.

References

- [1] V. Kavitha, K. Palanivelu, Degradation of nitrophenols by Fenton and photo-Fenton process, J. Photochem. Photobiol. A: Chem. 170 (2005) 83–95.
- [2] M. Ksibi, A. Zemzemi, R. Bouckchina, Photocatalytic degradability of substituted phenols over UV irradiated TiO₂, J. Photochem. Photobiol. A: Chem. 159 (2003) 61–70.
- [3] P.S. Mukherjee, A.K. Ray, Major challenges in the design of a large-scale photocatalytic reactor for water treatment, Chem. Eng. Technol. 22 (1999) 253–260.
- [4] K. Nakano, E. Obuchi, S. Takagi, R. Yamamot, T. Tanizaki, M. Taketomi, M. Eguchi, K. Ichida, S.M.A. Hashimoto, Photocatalytic treatment of water containing dinitrophenol and city water over TiO₂/SiO₂, Sep. Purif. Technol. 34 (2004) 67-72.
- [5] Ministry of the Environment of Japan PRTR data, [http://www.env.go.jp/prtr/](http://www.env.go.jp/prtr/prtrinfo/contents/2007/html_jp/T1_2007992000.htm) prtrinfo/contents/2007/html jp/T1 2007992000.htm, 2007.
- [6] J. Chen, D.F. Ollis, W.H. Rulkens, H. Bruning, Photocatalyzed oxidation of alcohols and organochlorides in the presence of native $TiO₂$ and metallized $TiO₂$ suspensions. Part I. Photocatlytic activity and pH influence, Water Res. 33 (1999) 661–668.
- [7] M.T. Hoffmann, S.T. Martin, W. Choi, D.W. Bahnemann, Environmental applications of semiconductor photocatalysis, Chem. Rev. 95 (1995) 69–96.
- [8] S. Fukinbara, F. Shiraishi, Characteristics of the photocatalytic reactor with an annular array of glass tubes surrounding a light source. 2. Kinetic analysis, CELSS J. 13 (2001) 11–23.
- [9] S. Fukinbara, F. Shiraishi, K. Nakano, Characteristics of the photocatalytic reactor with an annular array of glass tubes surrounding a light source. 1. Selection of a light source and photocatalyst support, CELSS J. 13 (2001) 1–10.
- [10] I.J. Ochuma, R.P. Fishiwick, J. Wood, J.M. Winerbottom, Photocatalytic oxidation of 2,4,6-trichlorophenol in water using a concurrent downflow contactor reactor (CDCR), J. Hazard. Mater. 144 (2007).
- [11] D.K. Lee, S.C. Kim, I.C. Cho, S.J. Kim, S.W. Kin, Photocatalytic oxidation of microcystin-LR in a fluidized bed reactor having TiO₂-coated activated carbon, Sep. Purif. Technol. 59–66 (2004).
- [12] Y.J. Li, X.D. Li, J.W. Li, J. Yin, photocatalytic degradation of methyl orange by TiO₂coated activated carbon and kinetic study, Water Res. 40 (2006) 1119–1126.
- [13] F. Shiraishi, T. Nomura, S. Yamaguchi, Y. Ohbuchi, Rapid removal of trace HCHO from indoor air by an air purifier consisting of a continuous concentrator and photocatalytic reactor and its computer simulation, Chem. Eng. J. 127 (2007) 157–165.
- [14] F. Shiraishi, S. Yamaguchi, Y. Ohbuchi, A rapid treatment of formaldehyde in a highly-tight room using a photocatalytic reactor combined with a continuous adsorption and desorption apparatus, Chem. Eng. Sci. 58 (2003) 929–934.
- [15] X. Cao, Y. Oda, F. Shiraishi, Photocatalytic and adsorptive treatment of 2,4dinitrophenol using a TiO₂ film covering activated carbon surface, Chem. Eng. J. 156 (2010) 98–105.
- [16] F. Shiraishi, S. Ikeda, N. Kamikariya, Photocatalytic decompositions of gaseous HCHO over thin films of anatase titanium oxide converted from amorphous in a heated air and in a aqueous solution of hydrogen peroxide, Chem. Eng. J. 148 (2009) 234–241.
- [17] F. Shiraishi, C. Kawanishi, Effect of diffusional film on formation of hydrogen peroxide in photocatalytic reaction, J. Phys. Chem. A 108 (2004) 10491–10496.
- [18] F. Shiraishi, M. Nagano, S.P. Wang, Characterization of a photocatalytic reaction in a continuous-flow recirculation reactor system, J. Tech. Biotechnol. 81 (2006) 1039–1048.
- [19] F. Shiraishi, T. Nakasako, Z.Z. Hua, Formation of hydrogen peroxide in photocatalytic reactions, J. Phys. Chem. A 107 (2003) 11072–11081.
- [20] S. Wang, F. Shiraishi, M. Nagano, Decomposition of formic acid in a photocatalytic reactor with a parallel array of four light sources, J. Chem. Technol. Biotechnol. 77 (2002) 805–810.
- [21] S. Wang, F. Shiraishi, K. Nakano, A synergistic effect of photocatalysis and ozonation on decomposition of formic acid in an aqueous solution, Chem. Eng. J. 87 (2002) 261–271.
- [22] S. Fukinbara, F. Shiraishi, H. Nagasue, A mathematical model for batchrecirculation reactor systems and its numerical calculation method, CELSS J. 12 (2000) 9–18.
- [23] M.G. White, O. Bensalem, W.R. Ernst, The mathematical modeling of batch recirculation reactors for kinetics studies, Chem. Eng. J. 25 (1982) 223–227.
- [24] F. Shiraishi, Computational Methods for Analysis of Immobilized Enzyme Reactions: From Reaction Kinetics to Reactor-Design Methods, Corona Publishing Co, Tokyo, 1997.
- [25] F. Shiraishi, M. Hiromitsu, T. Hasegawa, S. Kasai, A computational method for determination of the mass-transfer coefficient in packed-bed immobilized enzyme reactors, J. Chem. Technol. Biotechnol. 66 (1996) 405–413.
- [26] F. Shiraishi, K. Toyoda, H. Miyakawa, Decomposition of gaseous formaldehyde in a photocatalytic reactor with a parallel array of light sources. 2. Reactor performance, Chem. Eng. J. 114 (2005) 148–151.